## **Description of Additional Supplementary Files**

**Supplementary Movie 1**: Electron tomography reconstruction of a 160 nm-sized experimental supraparticle composed of 8,130 disk-shaped EuF<sub>3</sub> NPLs.

**Supplementary Movie 2**: Electron tomography reconstruction of a 183 nm-sized experimental supraparticle composed of disk-shaped EuF<sub>3</sub> NPLs.

**Supplementary Movie 3**: Electron tomography reconstruction of a supraparticle composed of triangular-shaped LaF<sub>3</sub> NPLs.

**Supplementary Movie 4**: Electron tomography reconstruction of a 180 nm-sized supraparticle composed of leaf-shaped GdF<sub>3</sub> NPLs.

**Supplementary Movie 5**: Electron tomography reconstruction of a 122 nm-sized supraparticle composed of leaf-shaped GdF<sub>3</sub> NPLs.

**Supplementary Data 1**: An experimental supraparticle composed of 8,130 EuF<sub>3</sub> disk-shaped nanoplatelets and its corresponding FFT pattern. The colour indicates the particle orientation.

**Supplementary Data 2**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.5 and a roundness of 0.9. The colour indicates the platelet orientation.

**Supplementary Data 3**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.5 and a roundness of 0.8. The colour indicates the platelet orientation.

**Supplementary Data 4**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.5 and a roundness of 0.7. The colour indicates the platelet orientation.

**Supplementary Data 5**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.5 and a roundness of 0.6. The colour indicates the platelet orientation.

**Supplementary Data 6**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.5 and a roundness of 0.5. The colour indicates the platelet orientation.

**Supplementary Data 7**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.5 and a roundness of 0.4. The colour indicates the platelet orientation.

**Supplementary Data 8**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.5 and a roundness of 0.3. The colour indicates the platelet orientation.

**Supplementary Data 9**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.5 and a roundness of 0.2. The colour indicates the platelet orientation.

**Supplementary Data 10**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.5 and a roundness of 0.1. The colour indicates the platelet orientation.

**Supplementary Data 11**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.5 and a roundness of 0 (perfect oblate hard spherocylinders). The colour indicates the platelet orientation.

**Supplementary Data 12**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.1 and a roundness of 0.3. The colour indicates the platelet orientation.

**Supplementary Data 13**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.2 and a roundness of 0.3. The colour indicates the platelet orientation.

**Supplementary Data 14**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.3 and a roundness of 0.3. The colour indicates the platelet orientation.

**Supplementary Data 15**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.4 and a roundness of 0.3. The colour indicates the platelet orientation.

**Supplementary Data 16**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.6 and a roundness of 0.3. The colour indicates the platelet orientation.

**Supplementary Data 17**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.7 and a roundness of 0.3. The colour indicates the platelet orientation.

**Supplementary Data 18**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.8 and a roundness of 0.3 and corresponding FFT pattern, exhibiting an icosahedral symmetry. The colour indicates the platelet orientation.

**Supplementary Data 19**: A simulated supraparticle composed of 1,000 disk-shaped platelets with an aspect ratio of 0.9 and a roundness of 0.3 and corresponding FFT pattern, exhibiting an icosahedral symmetry. The colour indicates the platelet orientation.

**Supplementary Data 20**: A simulated supraparticle composed of 500 disk-shaped platelets with an aspect ratio of 0.3 and a roundness of 0.5. The colour indicates the platelet orientation.

**Supplementary Data 21**: A simulated supraparticle composed of 2,000 disk-shaped platelets with an aspect ratio of 0.3 and a roundness of 0.5. The colour indicates the platelet orientation.

**Supplementary Data 22**: A simulated supraparticle composed of 2,000 disk-shaped platelets with an aspect ratio of 0.5 and a roundness of 0.5. The colour indicates the platelet orientation.